

## Philosophy 148 — Announcements & Such

- Branden will have office hours on Tuesday May 13 from 2-4.
- Raul will have a review for the final on Thurs. 5/15 @ 6pm (room TBA).
- Before next Tuesday, I will distribute some extra-credit problems (which will be due at the final). These will be worth 100 homework points.
- The final exam is **Tuesday, May 20 @ 8am @ 20 Barrows**.
  - I will hold a review session for the final exam — the day before the final (May 19). It will take place **May 19 @ 4-6pm @ 122 Wheeler**.
  - Before next Tuesday, I will be distributing a “sample” final exam.
- Today's Agenda
  - The Grue Paradox (aftermath — and consequences for IL and IE)
  - Farewell
  - Course Evaluations

## “Carnapian” Counterexamples to (NC) and (M)

(K) Either: ( $H$ ) there are 100 black ravens, no nonblack ravens, and 1 million other things, or ( $\sim H$ ) there are 1,000 black ravens, 1 white raven, and 1 million other things.

- Let  $E \stackrel{\text{def}}{=} Ra \ \& \ Ba$  ( $a$  randomly sampled from universe). Then:

$$\Pr(E \mid H \ \& \ K) = \frac{100}{1000100} \ll \frac{1000}{1001001} = \Pr(E \mid \sim H \ \& \ K)$$

- $\therefore$  This  $K/\Pr$  constitute a counterexample to (NC), assuming a “Carnapian” theory of confirmation. This model can be emulated in the later Carnapian  $\lambda/\gamma$ -systems [13].

- Let  $Bx \stackrel{\text{def}}{=} x$  is a black card,  $Ax \stackrel{\text{def}}{=} x$  is the ace of spades,  $Jx \stackrel{\text{def}}{=} x$  is the jack of clubs, and  $K \stackrel{\text{def}}{=} a$  card  $a$  is sampled at random from a standard deck (where  $\Pr$  is also standard):

- $\Pr(Aa \mid Ba \ \& \ K) = \frac{1}{26} > \frac{1}{52} = \Pr(Aa \mid K).$
- $\Pr(Aa \mid Ba \ \& \ Ja \ \& \ K) = 0 < \frac{1}{52} = \Pr(Aa \mid K).$

## A “Carnapian” Counterexample to $(\ddagger)$

- (K) Either: ( $H_1$ ) there are 1000 green emeralds 900 of which have been examined before  $t$ , no non-green emeralds, and 1 million other things in the universe, or ( $H_2$ ) there are 100 green emeralds that have been examined before  $t$ , no green emeralds that have not been examined before  $t$ , 900 non-green emeralds that have not been examined before  $t$ , and 1 million other things.
- Imagine an urn containing true descriptions of each object in the universe ( $\text{Pr} \stackrel{\text{def}}{=} \text{urn model}$ ). Let  $\mathcal{E} \stackrel{\text{def}}{=} “Ea \& Oa \& Ga”$  be drawn.  $\mathcal{E}$  confirms  $H_1$  but  $\mathcal{E}$  *disconfirms*  $H_2$ , relative to  $K$ :

$$\text{Pr}(\mathcal{E} \mid H_1 \& K) = \frac{900}{1001000} > \frac{100}{1001000} = \text{Pr}(\mathcal{E} \mid H_2 \& K)$$

- This  $K/\text{Pr}$  constitute a counterexample to  $(\ddagger)$ , assuming a “Carnapian” theory of confirmation. This probability model can be emulated in the later Carnapian  $\lambda/\gamma$ -systems [13].

# Is “Grue” an Observation Selection Effect? Part I

- **Canonical Example of an OSE:** I use a fishing net to capture samples of fish from various (randomly selected) parts of a lake. Let  $E$  be the claim that all of the sampled fish were over one foot in length. Let  $H$  be the hypothesis that all the fish in the lake are over one foot  $[(\forall x)((Fx \ \& \ Lx) \supset O x)]$ .
- Intuitively, one might think  $E$  should evidentially support  $H$ . This may be so for an agent who knows *only* the above information ( $K$ ) about the observation process. That is, it seems plausible that  $\Pr(E \mid H \ \& \ K) > \Pr(E \mid \sim H \ \& \ K)$ , where  $\Pr$  is taken to be “evidential” (or “epistemic”) probability.
- But, what if I *also* tell you that ( $D$ ) the net I used to sample the fish from the lake (which generated  $E$ ) has holes that are all over one foot in diameter? It seems that  $D$  *defeats* the support  $E$  provides for  $H$  (relative to  $K$ ), because  $D$  *ensures*  $O$ . Thus, intuitively,  $\Pr(E \mid H \ \& \ D \ \& \ K) = \Pr(E \mid \sim H \ \& \ D \ \& \ K)$ .

## Is “Grue” an Observation Selection Effect? Part II

- Note: the “grue” hypothesis ( $H_2$ ) entails the following claim, which is not entailed by the green hypothesis ( $H_1$ ):
  - ( $H'$ ) All green emeralds have been (or will have been) examined prior to  $t$ .  $[(\forall x)((Ex \ \& \ Gx) \supset O_x)]$ .
- Now, consider the following two observation processes:
  - **Process 1.** For each green emerald in the universe, a slip of paper is created, on which is written a true description of that object as to whether it has property  $O$ . All the slips are placed in an urn, and one slip is sampled at random from the urn. By *this* process, we learn ( $\mathcal{E}$ ) that  $Ea \ \& \ Ga \ \& \ Oa$ .
  - **Process 2.** Suppose all the green emeralds in the universe are placed in an urn. We sample an emerald ( $a$ ) at random from this urn, and we examine it. [We know *antecedently* that the examination of  $a$  will take place prior to  $t$ , *i.e.*, that  $Oa$  is true.] By *this* process, we learn ( $\mathcal{E}$ ) that  $Ea \ \& \ Ga \ \& \ Oa$ .
- Goodman seems to presuppose Process 2 in his set-up.

## What Could “Carnapian” Inductive Logic Be? Part I

- The early Carnap dreamt that probabilistic inductive logic (confirmation theory) could be formulated in such a way that it *supervenes* on deductive logic in a *very strong* sense.
  - **Strong Supervenience (SS)**. All confirmation relations involving sentences of a first-order language  $\mathcal{L}$  supervene on the deductive relations involving sentences *of*  $\mathcal{L}$ .
- Hempel clearly saw (SS) as a *desideratum* for confirmation theory. The early Carnap also seems to have (SS) in mind.
- I think it is fair to say that Carnap’s project — understood as requiring (SS) — was unsuccessful. [I think *this* is true for reasons that are *independent* of “grue” considerations.]
- The later Carnap seems to be aware of this. Most commentators interpret this shift as the later Carnap simply *giving up* on inductive logic (*qua logic*) altogether.
- I want to resist this “standard” reading of the history.

## What Could “Carnapian” Inductive Logic Be? Part II

- I propose a different reading of the later Carnap, which makes him much more coherent with the early Carnap.
- I propose *weakening* the supervenience requirement in such a way that it (a) ensures this coherence, and (b) maintains the “logicality” of confirmation relations in Carnap’s sense.
- Let  $\mathcal{L}$  be a formal language strong enough to express the fragment of probability theory Carnap needs for his later, more sophisticated confirmation-theoretic framework.
  - **Weak Supervenience (WS).** All confirmation relations involving sentences of a first-order language  $\mathcal{L}$  supervene on the deductive relations involving sentences *of*  $\mathcal{L}$ .
- As it turns out,  $\mathcal{L}$  needn’t be very strong (in fact, one can get away with PRA!). So, even by early (*logician*) Carnapian lights, satisfying (WS) is all that is *really* required for “logicality”.
- The specific (WS) approach I propose takes confirmation to be a *four*-place relation: between  $E$ ,  $H$ ,  $K$ , and a function  $\text{Pr}$ .


## What Could “Carnapian” Inductive Logic Be? Part III

- Consequences of moving to a 4-place confirmation relation:
  - We need not try to “construct” “logical” probability functions from the syntax of  $\mathcal{L}$ . This is a dead-end anyhow.
  - Indeed, on this view, inductive logic has nothing to say about the *interpretation/origin* of Pr. That is *not* a *logical* question, but a question about the *application* of logic.
    - Analogy: Deductive logicians don’t owe us a “logical interpretation” of the truth value assignment function  $v$ .
  - Moreover, this leads to a vast increase in the *generality* of inductive logic. Carnap was stuck with an impoverished set of “logical” probability functions (in his  $\lambda/\gamma$ -continuum).
    - On my approach, *any* probability function can be part of a confirmation relation. Which functions are “suitable” or “appropriate” or “interesting” will depend on *applications*.
    - So, some confirmation relations will not be “interesting”, *etc.* But, this is (already) true of *entailments*, as Harman showed.
  - Questions: Now, what *is* the job of the inductive logician, and how (if at all) do they interact with *epistemologists*?

## What Could “Carnapian” Inductive Logic Be? Part IV


- The inductive logician must explain how it is that inductive logic can satisfy the following Carnapian *desiderata*.
  - The confirmation function  $c(H, E | K)$  quantifies a *logical* (in a Carnapian sense) relation among statements  $E$ ,  $H$ , and  $K$ .
    - ( $\mathcal{D}_1$ ) One aspect of “logicality” is ensured by moving from (SS) to (WS) [from an  $\mathcal{L}$ -determinate to an  $\mathcal{L}$ -determinate concept].
    - ( $\mathcal{D}_2$ ) Another aspect of “logicality” insisted upon by Carnap is that  $c(H, E | K)$  should *generalize* the entailment relation.
      - This means (at least) that we need  $c(H, E | K)$  to take a maximum (minimum) value when  $E \& K \models H$  ( $E \& K \models \sim H$ ).
      - Very few *relevance* measures  $c$  satisfy this “generalizing  $\models$ ” requirement. That’s another job for the inductive logician.
  - ( $\mathcal{D}_3$ ) There must be *some* interesting “bridge principles” linking  $c$  and *some* relations of evidential support, in *some* contexts.
    - ( $\mathcal{D}_2$ ) implies that *if* there are any such bridge principles linking *entailment* and *conclusive evidence*, these should be *inherited by*  $c$ . This brings us back to Harman’s problem!

## Three Salient Quotes from Goodman [7]

 The “new riddle” is *about inductive logic (not epistemology)*.

**Quote #1** (page 67): “Just as deductive logic is concerned primarily with a relation between statements — namely the consequence relation — that is independent of their truth or falsity, so inductive logic ... is concerned primarily with a comparable relation of confirmation between statements. Thus the problem is to define the relation that obtains between any statement  $S_1$  and another  $S_2$  if and only if  $S_1$  may properly be said to confirm  $S_2$  in any degree.”

**Quote #2** (73): “Confirmation of a hypothesis by an instance depends ... upon features of the hypothesis other than its syntactical form”.

 But, Goodman’s *methodology* appeals to *epistemic* intuitions.

**Quote #3** (page 73): “... the fact that a given man now in this room is a third son *does not increase the credibility of* statements asserting that other men now in this room are third sons, *and so does not confirm* the hypothesis that all men now in this room are third sons.”