

# A Historical Introduction to Confirmation Theory

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- Here's what Nicod [23] *said* about instantial confirmation:

*Consider the formula or the law: A entails B. How can a particular proposition, or more briefly, a fact, affect its probability? If this fact consists of the presence of B in a case of A, it is favourable to the law ... on the contrary, if it consists of the absence of B in a case of A, it is unfavourable to this law.*

- By “is (un)favorable to”, Nicod meant “raises (lowers) the inductive probability of”. Here, Nicod has in mind *Keynesian* inductive probability (more on *that* later).
- While Nicod is not very clear on the logical details (stay tuned for Hempel!), some things are clear in what he says:
  - Instantial confirmation is a relation between singular and general propositions/statements (“facts” and “laws”).
  - $\pm$ Confirmation consists in  $\pm$ *probabilistic relevance*.
  - Positive instances confirm; negative instances disconfirm.

- When Hempel [16] logically reconstructs Nicod's inchoate remarks about instantial confirmation, some things get lost.
- For instance, *probability* completely falls out of Hempel's reconstruction of Nicod. And, he reconstructs Nicod as describing a relation between *objects* and propositions.
- Hempel's initial, formal reconstruction of "Nicod's Criterion" for instantial confirmation is as follows:
 

(NC<sub>0</sub>) An object  $a$  confirms a universal generalization of the form  $\ulcorner (\forall y)(\phi y \supset \psi y) \urcorner$  iff  $a$  exemplifies both  $\phi$  and  $\psi$ .
- Rendering "A entails B" as  $\ulcorner (\forall y)(\phi y \supset \psi y) \urcorner$  is charitable.
- But, the rest of (NC<sub>0</sub>) just *can't* be what Nicod had in mind (e.g., probability is *non-monotonic* — more on that below). Also, (NC<sub>0</sub>) is clearly absurd, as Hempel makes very clear.
- According to (NC<sub>0</sub>), if " $Ra \ \& \ Ba$ " is true, then  $a$  will confirm " $(\forall y)(Ry \supset By)$ ", but *nothing* can confirm the *logically equivalent* claim " $(\forall y)[(Ry \ \& \ \sim By) \supset (Ry \ \& \ \sim Ry)]$ "!
- I'll say a lot more about "Nicod's Criterion" tomorrow.

- Hempel proceeded to formulate a precise, logical theory of confirmation as a relation between sentences in first-order languages. He was inspired by Nicod's *instantial idea*.
- Hempel begins by making precise the informal Nicodian idea of a “conforming instance”. He starts with the notion of *the E-development of a hypothesis H*:  $\text{dev}_E(H)$ .
- $\text{dev}_E(H)$  is constructed from the instances of  $H$  with respect to the individual constants appearing in  $E$ . *E.g.*:
  - Let  $E = Ra \ \& \ Ba$ , and  $H = (\forall y)(Ry \supset By)$ . The set of  $E$ -instances of  $H$  is the singleton  $\{Ra \supset Ba\}$ . And,  $\text{dev}_E(H)$  is the *conjunction* of  $H$ 's  $E$  instances, which is just  $Ra \supset Ba$ .
  - Generally,  $\text{dev}_E(H)$  will be the conjunction (disjunction) of the  $E$ -instances of  $H$  if  $H$  is a universal (existential) claim. And, if  $H$  is neither a  $\forall$  nor a  $\exists$  sentence, then  $\text{dev}_E(H) = H$ .
- Hempel's basic idea:  $E$  (directly) confirms  $H$  if  $E \vdash \text{dev}_E(H)$ .
- On this account,  $Ra \ \& \ Ba$  confirms  $(\forall y)(Ry \supset By)$ . But, so does  $\sim Ra \ \& \ \sim Ba$  (more tomorrow!). Indeed, the only claim that *disconfirms*  $H$  is  $Ra \ \& \ \sim Ba$ . Very Nicodian (*sans Pr*)!

- Hempel's confirmation relation has various properties. Most notably, his conception satisfies the *equivalence condition*:  
(EQC) If  $E$  confirms  $H$  and  $H \dashv\vdash H'$ , then  $E$  confirms  $H'$ .
- Recall, Hempel's reconstruction of Nicod ( $NC_0$ ) did not satisfy the (analogous) equivalence condition (absurd?).
- Hempel's relation also has the following properties:
  - (EC) If  $E \vdash H$ , then  $E$  confirms  $H$ .
  - (SCC) If  $E$  confirms  $H$  and  $H \vdash H'$ , then  $E$  confirms  $H'$ .
  - (M) If  $E$  confirms  $H$  and  $E' \vdash E$ , then  $E'$  confirms  $H$ .
  - (CC) If  $E$  confirms both  $H$  and  $H'$ , then  $H$  and  $H'$  are consistent.
- (M) plays a key role in the ravens paradox (more on that tomorrow). We'll talk more about these properties below.
- Hempel's theory *lacks* certain other properties, such as:  
(CCC) If  $E$  confirms  $H$  and  $H' \vdash H$ , then  $E$  confirms  $H'$ .
- Before we get to *probabilistic* accounts of confirmation, we'll look briefly at "Hypothetico-Deductive" (HD) confirmation.

- The (naïve) idea behind (HD) seems to be that science works by *deducing predictions* ( $E$ ) from hypotheses ( $H$ ).
- Thus, in a case where  $H \vdash E$ , if we observe that  $E$  obtains, then this (“correct prediction”) *confirms*  $H$ , and if we observe that  $E$  fails to obtain, then this *disconfirms*  $H$ .
- *I.e.*, if  $H \vdash E$ , then  $E$  HD-confirms  $H$  [ $\sim E$  HD-disconfirms  $H$ ].
- (HD)-confirmation *satisfies* (CCC), but *violates* (EC), (SCC), (M), and (CC). Very *non-Hempel*ian! [They agree on (EQC).]
- (HD)-confirmation has other problems of its own:
  - **Duhem–Quine.** *Auxiliary assumptions* ( $A$ ) are always needed for the *deduction* of predictions ( $E$ ). How do we *apportion* praise/blame between  $H$  and  $A$ , when  $E/\sim E$  is observed?
  - **Irrelevant Conjunction.** If  $E$  HD-confirms  $H$ , then  $E$  also HD-confirms  $H \& X$ , even if  $X$  is utterly irrelevant to  $H$ ,  $E$ . [Hempel’s theory has a similar “problem”, since if  $E$  Hempel-confirms  $H$ , then so does  $E \& X$ , for *any*  $X$  (M!).]
- OK, enough about deductive-logical approaches to confirmation. Let’s look at some *probabilistic* accounts.

- Nicod's early intuition was that confirmation had to do with *probability-raising*. And, contemporary Bayesians have come back around to this view. What happened in between?
- In the first edition of LFP, Carnap [3] undertakes a precise probabilistic explication of the concept of confirmation.
- Carnap was interested not only in the qualitative confirmation relation. He also wanted explications of comparative and quantitative confirmation concepts.
  - **Qualitative.**  $E$  inductively supports  $H$ .
  - **Comparative.**  $E$  supports  $H$  *more strongly than*  $E'$  supports  $H'$ .
  - **Quantitative.**  $E$  inductively supports  $H$  to degree  $r$ .
- Carnap begins by clarifying the *explicandum* (the confirmation concept) in various ways, including:
  - Qualitative.**  $(\star)$   $E$  gives some (positive) evidence for  $H$ .
- Note two things. First,  $(\star)$  sounds *epistemic* (not *logical*). Second,  $(\star)$  sounds like it involves (positive) *relevance*.
- Strangely, Carnap proceeds (in LFP<sub>1</sub>) to offer a *logical* account of confirmation that does *not* involve relevance...

- In the 1st ed. of LFP, Carnap characterizes “the degree to which  $E$  confirms  $H$ ” as  $c(H, E) = \Pr(H | E)$ , which leads to:
  - Quantitative.**  $\Pr(H | E) = r$ .
  - Comparative.**  $\Pr(H | E) > \Pr(H' | E')$ .
  - Qualitative.**  $\Pr(H | E) > t$  (for some “threshold value”  $t$ ).
    - Doesn't sound like  $(\star)$ . More on this dissonance below.
- Like Hempel, Carnap wanted a *logical* explication of confirmation (as a relation between sentences in FOLs).
- For Carnap, this meant that the probability functions used in confirmation theory must *themselves* be “logical”.
- This leads naturally to the Carnapian project of providing a “logical explication” of conditional probability  $\Pr(\cdot | \cdot)$  *itself*.
- Note: Here, Carnap (like Nicod) was influenced by Keynes [20], who believed that there were “partial entailments” out there in logical space. I'm skeptical (as are most Bayesians).
- *Even if* there are “logical probabilities”, are they *required* for a *logical* conception of confirmation *based on* probability? I'll come back to that. Continuing with Carnapian  $c \dots$

- Later in LFP<sub>1</sub>, Carnap gives counterexamples to Hempel's (SCC), which presupposes a more (★)-like **qualitative** conception of confirmation. There, he presupposes:

**Qualitative.**  $E$  confirms  $H$  iff  $\Pr(H | E) > \Pr(H | \top)$ .

- This *probabilistic relevance* conception *violates* (SCC), whereas the previous Pr-threshold conception *implies* (SCC).
- The second edition of LFP [4] includes a preface which acknowledges an “*ambiguity*” in LFP<sub>1</sub>, and concedes that the (**qualitative**) relevance conception is “more interesting”.

- **Firmness.** The degree to which  $E$  confirms <sub>$f$</sub>   $H$ :

$$c_f(H, E) = \Pr(H | E).$$

- **Increase in Firmness.** The degree to which  $E$  confirms <sub>$i$</sub>   $H$ :

$$c_i(H, E) = f[\Pr(H | E), \Pr(H | \top)]$$

$f$  measures “the degree to which  $E$  *increases* the Pr of  $H$ .”

- The 1st ed. of LFP was mainly about firmness, and the 2nd edition only adds the preface, which says very little about  $c_i$ . Specifically, no function  $f$  is rigorously defended there.

- Many candidate functions  $f$  satisfy the *relevance* constraint:
  - ( $\mathcal{R}$ )  $f[\Pr(H | E), \Pr(H | \top)] \geq 0$  iff  $\Pr(H | E) \geq \Pr(H | \top)$
- The three historically most popular such functions  $f$  are:
  - $d(H, E) = \Pr(H | E) - \Pr(H | \top)$
  - $r(H, E) = \log \left[ \frac{\Pr(H | E)}{\Pr(H | \top)} \right]$
  - $l(H, E) = \log \left[ \frac{\Pr(H | E)(1 - \Pr(H | \top))}{(1 - \Pr(H | E)) \Pr(H | \top)} \right] = \log \left[ \frac{\Pr(E | H)}{\Pr(E | \sim H)} \right]$
- Interestingly, these measures are *not comparatively equivalent*. They disagree on many comparative claims.
- The most radical (and interesting) disagreement between these measures occurs in the context of *favoring* claims [9] of the form  $c(H, E) \geq c(H', E)$ . For instance, only  $l$  satisfies:
  - If  $E \vdash H$  and  $E \not\vdash H'$ , then  $c(H, E) \geq c(H', E)$ .
- Only  $r$  satisfies:  $\Pr(E | H) > \Pr(E | H') \Rightarrow c(H, E) > c(H', E)$ .
- I'll say more about disagreement between (these and other) relevance measures below (and next week). Back to Carnap.

- From an inductive-logical point of view, confirmation measures should *quantitatively generalize* entailment:
  - ( $\mathcal{D}$ ) Provided that both  $E$  and  $H$  are *contingent* claims<sup>1</sup>
    - $c_i(H, E)$  should be *maximal* if  $E \vdash H$ , and *minimal* if  $E \vdash \sim H$ . [Note:  $\text{Pr}(H | E)$  satisfies *this*, but *not*  $\mathcal{R}$ .]
- Kemeny & Oppenheim [19] used this consideration (and others) to argue that the best explication of  $c_i(H, E)$  is:

$$F(H, E) = \frac{\text{Pr}(E | H) - \text{Pr}(E | \sim H)}{\text{Pr}(E | H) + \text{Pr}(E | \sim H)} \doteq l(H, E)$$

- $F$  can be expressed as a function  $f$  of  $\text{Pr}(H | E)$  and  $\text{Pr}(H | \top)$ , and it satisfies  $\mathcal{R}$ ,  $\mathcal{D}$ , and various other IL desiderata.
- One can use  $F$  to define **comparative** [ $F(H, E) > F(H', E')$ ] and **qualitative** [ $F(H, E) > 0$ ] confirmation <sub>$i$</sub>  concepts.
- I think  $F$  (or any comparative equivalent, like  $l$ ) has the proper *form* for an *inductive-logical* relevance measure of degree of confirmation. Whither (relevance) inductive logic?

<sup>1</sup>Here, I'm bracketing the “paradox of entailment” cases, which are tricky.

Theory	Does Theory have property?					
	EQC	EC	CC	M	SCC	CCC
Nicodian “Instantial”	NO	NO? <sup>1</sup>	YES? <sup>1</sup>	YES? <sup>1</sup>	NO	NO
Hempelian “Instantial”	YES	YES	YES <sup>2</sup>	YES	YES	NO
Hypothetico-Deductivism	YES	NO	NO	NO	NO	YES
Firmness	YES	YES <sup>3</sup>	NO	NO	YES	NO
Increase in Firmness	YES	YES <sup>4</sup>	NO	NO	NO	NO

The last row — three counterexamples for increase in firmness:

- (CC)  $E$  = card is black,  $H$  = card is the  $A\spadesuit$ ,  $H'$  = card is the  $J\clubsuit$ .  $E$  confirms both  $H$  and  $H'$ , even though they are inconsistent.
- (SCC)  $E$  = card is black,  $H$  = card is the  $A\spadesuit$ , and  $H'$  = card is an ace.
- (CCC)  $E$  = card is the  $A\spadesuit$ ,  $H$  = card is an ace, and  $H'$  = card is the  $A\blacklozenge$ .

<sup>1</sup>Nicod’s theory may not come down clearly on these (or it may *trivially*).

<sup>2</sup>Assuming that  $E$  is not self-contradictory.

<sup>3</sup>Assuming that  $\Pr(E | K) \neq 0$ .

<sup>4</sup>Assuming that  $\Pr(H | K) \in (0, 1)$ , and  $\Pr(E | K) \in (0, 1)$ .

- Another popular relevance measure from the literature is:

$$s(H, E) = \Pr(H | E) - \Pr(H | \sim E)$$

- Six properties of measures  $c$  (for contingent  $H, E$ ), see [7]:
  - If  $E \vdash H$  and  $E \not\vdash H'$ , then  $c(H, E) \geq c(H', E)$ .
  - If  $\Pr(E | H) > \Pr(E | H')$ , then  $c(H, E) > c(H', E)$ .
  - If  $\Pr(H | E) > \Pr(H | E')$ , then  $c(H, E) > c(H, E')$ .
  - $c(H, E) = c(E, H)$
  - $c(H, E) = -c(H, \sim E)$
  - $c(H, E) = -c(\sim H, E)$

Relevance Measure	Does Measure have property?					
	(1)	(2)	(3)	(4)	(5)	(6)
$d(H, E)$	NO	NO	YES	NO	NO	YES
$r(H, E)$	NO	YES	YES	YES	NO	NO
$l(H, E)$	YES	NO	YES	NO	NO	YES
$s(H, E)$	NO	NO	NO	NO	YES	YES

- Carnap (and Keynes) sought a more general theory of argument evaluation/goodness — “inductive soundness”.
- Assessing the “goodness” (*soundness*) of a *deductive* argument from  $E$  to  $H$  requires the determination of:
  - Whether the argument is valid. [logical]
  - Whether  $E$  is true. [(generally) non-logical]
- How do we *generalize* this to include the *inductive* case?
- Of course, we *still* have to determine whether  $E$  is true.
- What *else*? Carnap would say we need to determine “the degree to which  $E$  confirms  $H$ .” But, he would also say that this determination must be made in accordance with:  
**The Requirement of Total Evidence.** In the application of IL to a given knowledge situation, the total evidence available must be taken as a basis for determining the degree of confirmation.
- For Carnap, “take  $E$  as a basis” means “conditionalize Pr on  $E$ .” Problem: let  $K_C$  express “everything we (assessor) know.” Then, if we know  $E$ ,  $\Pr(H \mid E \ \& \ K_C) = \Pr(H \mid K_C)$ !

- Therefore, if we know that  $E$  is true, we *cannot* — on a Carnapian approach — determine that  $E$  confirms <sub>$i$</sub>   $H$ .
- This is problematic. The non-logical component of our all things considered assessment of the argument's "goodness" has *interfered* with its (Carnapian) logical component!
- This is *not* a problem for *firmness*, since it doesn't prevent the logical probability  $\Pr(H | E \& K_C) = \Pr(H | K_C)$  from being greater than a *threshold value*. This is *just* a problem for  $c_i$ .
- Bayesians face a similar problem: "old evidence" (on which more below). General problem: *no Pr-assignment such that  $\Pr(E) = 1$  can reflect a correlation between  $E$  and  $H$ .*
- Thus, it seems, any Pr-relevance based approach to confirmation (logical or otherwise!) will have to abandon the principle of total evidence, *as Carnap understood it*.
- If RTE does *not* imply that we should *conditionalize* our evaluative probability assignment on our total evidence, then what *does* it imply? Good question! First, Bayesian  $c \dots$

- Most modern Bayesians don't believe there are “logical” probabilities. I'm inclined to agree, but I won't dwell on it.
- As a result, most modern Bayesians simply *give up on* the traditional project of confirmation theory *as a branch of IL*.
- Instead, they set their sights on explicating an explicitly *epistemic* (and subjective) notion of “inductive support”:
  - **Qualitative.** *E* confirms *H* for agent *X* at time *t* iff *E* and *H* are positively correlated under *X*'s credence function at *t*.
- This is *formally* similar to the inductive-logical concept  $c_i$ . But, it is *subjective* and *epistemic*, *not* objective and logical.
- Like Carnap, Bayesians assume that *all confirmation relations supervene on one kind of probability*. They just disagree on **which kind** forms the supervenience base.
- There is controversy among Bayesians about **quantitative** and **comparative**  $c_i$ . I'll be talking about that next week (there's some interesting new psychological research here).
- Next: four views on the “logicality of Pr” (and the Carnapian/Bayesian supervenience assumption) ...

- **Adams/Hailperin** [1, 14]. Individual probability assignments appearing in inductive logic are *never* logical. The *logical* properties (in IL) must hold for *all* probability assignments.
  - ⇒ Inductive logic does *not* undergird assessments of the strength of *particular* arguments. Rather, inductive logic characterizes “probabilistically valid” forms ‘ $\phi_1, \dots, \phi_n \therefore \psi$ ’ such that  $\forall \text{Pr}$ :
 
$$\text{Pr}(\phi_1) \in \alpha_1, \dots, \text{Pr}(\phi_n) \in \alpha_n \models \text{Pr}(\psi) \in \beta$$
- **Carnap/Maher** [21]. Individual probability assignments that appear in confirmation functions ( $c_f/c_i$ ) are *always* logical. And, inductive logic/confirmation theory *does* undergird assessments of the (*logical*) strength of *particular* arguments (*via logical Pr*’s).
- **Subjective Bayesian**. Individual Pr assignments that appear in confirmation functions ( $c_f/c_i$ ) are *never* logical. Confirmation theory *does* undergird assessments of the (*epistemic/subjective*) “strength”/“weight” of *particular* arguments (*via subjective Pr*’s).
- **Alternative**. Individual Pr’s appearing in  $F_{\text{Pr}}(H, E)$  are *not always* logical (*or subjective*). IL/CT *does* undergird assessments of the strength of *particular* arguments *in contexts C*. Which Pr(s) are appropriate for a given assessment (generally) *depends on C*.

- Probabilistic relevance approaches to confirmation theory have had various “successes”, and problems of their own.
- On the “success” side, we have some interesting Pr-relevance “resolutions” of problems and paradoxes:
  - The Duhem–Quine problem. [6, 24, 11, 25, 12]
  - The irrelevant conjunction problem. [8, 15]
  - The ravens paradox [tomorrow!]. [10]
  - The value of varied/diverse evidence. [26]
  - The value of unification/coherence. [22, 2, 5]
  - Explanations of Kahneman & Tversky “fallacies” [next week!]
- I’d be happy to talk about any of these problems in detail (except the two problems I’ll be discussing later this trip!).
- Next, I’ll focus on the “old evidence” problem (for Bayesian confirmation), and how Bayesians have responded to it.
- Example: a highly reliable pregnancy test comes out + (for Mary). Call this evidence  $E$ . You learn  $E$ , and (in this context  $C$ ) you assign  $\Pr(E) = 1$ . So,  $E$  cannot confirm <sub>$i$</sub>  ( $H$ ) that Mary is pregnant (in context  $C$ ). There are 3 Bayesian responses.

- **Response 1.** The “look at another context  $C'$ ” response [17]:
  - OK, in your *actual* context  $C$  where you *know*  $E$ , you can't apply  $\text{confirmation}_i$ . So, think about *another* (historical, counterfactual, *etc.*) context  $C'$  in which you *do not know*  $E$ .
  - Then, see if your “counterpart's” credence function  $\text{Pr}'$  (or a “logical”  $\text{Pr}'$  *conditioned on their total evidence in  $C'$* ) reflects a correlation between  $E$  and  $H$  in  $C'$ , and then *expropriate*.
  - This seems bizarre to me. Why should what one would or should believe in  $C'$  bear on what one should believe in  $C$ ?
- **Response 2.** The “look at another evidence  $E'$ ” response [13]:
  - OK, you can't assess whether evidence  $E$  supports  $H$  in  $C$ . So, think about *another* evidential proposition  $E'$  (*e.g.*, that “ $H$  predicts  $E$  in  $C$ ”), and argue that  $E'$  supports  $H$  in  $C$ .
  - This one just *changes the subject*. It's  $E$  we're talking about.
- **Response 3.** The “use non-standard  $\text{Pr}$  theory” response [18]:
  - Move to a theory of probability that allows  $E$  and  $H$  to be “correlated” under  $\text{Pr}$ , *even if*  $E$  has probability 1 under  $\text{Pr}$ .
  - This avoids the two problems above. But, (a) it *disunifies*  $c_i$ -theory, (b) what if the pregnancy test *always* yields + results?, and (c) what if you *also* know  $H$  in  $C$  [ $\text{Pr}(H) = 1$ ]?

- I don't think any of these responses will work. My two take-away lessons from the “old evidence” problem (and the analogous problem for Carnapian increase in firmness) is:
  - The requirement of total evidence must not be interpreted as *requiring* that we (*always*) **conditionalize** evaluative (*i.e.*, confirmation-theoretic) probability assignments on everything we know (in the evaluative context).
  - Not all confirmation relations (in all contexts) supervene on credences (or logical probabilities, or any other kind of Pr).
- Note: In *some* contexts  $C$ , confirmation-theoretic probability assignments *should* assign  $\text{Pr}(E) = 1$ . *E.g.*, if the pregnancy test is *known to always* yield positive results in  $C$ .
- To my mind, the RTE just means that when making an assessment of argument strength, we should do so on the basis of everything we know. Thus, the RTE is not a very “helpful” principle from a methodological point of view.
- But, it is naïve to hope for “helpful” principles in this sense: either for credences or confirmation-theoretic probabilities.

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